

## ASSIGNMENT : COMPLEX NUMBER

Q1. Express in standard form : a+ib

a)  $(-\sqrt{-1})^{4n+3}$

b)  $i^n + i^{n+1} + i^{n+2} + i^{n+3}$

c)  $1+i^2+i^4+i^6+\dots+i^{20}$

d)  $(\sqrt{3} + \sqrt{-2})(2\sqrt{3}-i)$

e)  $(1-2i)^{-3}$

f)  $\frac{2-\sqrt{-25}}{1-\sqrt{-16}}$

Q2. Find x and y for  $\frac{x-1}{3+i} + \frac{y-1}{3-i} = i$   $\begin{bmatrix} x = -4 \\ y = 6 \end{bmatrix}$

Q3. Find x and y for which the complex No.  $-3+ix^2y$  and  $x^2+y+4i$  are conjugate of each other

$$\begin{bmatrix} x = 1 & y = -4 \\ x = -1 & y = -4 \end{bmatrix}$$

Q4. If  $\frac{(a+i)^2}{(2a-i)} = p+iq$  to show  $p^2+q^2 = \frac{(a^2+1)^2}{4a^2+1}$

Q5. If  $z_1, z_2$  are complex no. such that  $\frac{2z_1}{3z_2}$  is purely imaginary then

show  $\left| \frac{z_1 - z_2}{z_1 + z_2} \right| = 1$

Q6. If  $x = -5+4i$  show that the value of  $x^4 + 9x^3 + 35x^2 - x + 4$  is -160.

Q7. If  $iz^3 + z^2 - z + i = 0$  then show that  $|z| = 1$

Q8. Express in polar form.

a)  $\sin 120^\circ - i \cos 120^\circ$       b)  $\frac{2(i-1)}{1+i\sqrt{3}}$

Q9. Find  $\theta$  for complex No.  $\frac{1+i \cos \theta}{1-2i \cos \theta}$  is purely real.

Q10. Solve the Quad. Eqn (over C)

a)  $x^2 - \sqrt{2}ix + 12 = 0$   $[3\sqrt{2}i \ \& \ -2\sqrt{2}i]$

b)  $2x^2 + 3ix + 2 = 0$   $[\frac{i}{2} \ \& \ -2i]$

c)  $2x^2 - (3+7i)x - (3-9i) = 0$   $[\frac{3+i}{2} \ \& \ 3i]$

d)  $x^2 - (7-i)x + (18-i) = 0$   $[4-3i \ \& \ 3+2i]$