# **# SPECIAL FORMS OF 3D (LINE & PLANE)**

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#### FOR XII/CBSE/JEE/NDA

#### FORM-1 INTERSECTING LINES AND THEIR POINT OF INTERSECTION.

**Q.1** Show that the lines  $r=3i+2j-4k +\lambda(i+2j+2K)$  and  $r=5i-2j+\mu(3i+2j+6k)$  are INTERSECTING. Also find their point of intersection.

#### FORM-2 FOOT & IMAGE OF A POINT WITH A LINE.

**Q.2** Find the coordinates of the FOOT of perpendicular and the length of perpendicular drawn from the point P (5,4,2) to the line  $r = -i+3j+k+\lambda(2i+3j-k)$ . Also find its IMAGE in this line.

#### FORM-3 FOOT & IMAGE OF A POINT WITH A PLANE.

**Q.3** Find the coordinates of the FOOT of perpendicular and the perpendicular distance of the point P (3,2, 1) from the plane 2x-y+z+1=0. Also find its IMAGE in this plane.

### FORM-4 POINT OF INTERSECTION OF A LINE AND PLANE.

**Q.4** Find the distance of the point P (2, 12, 5) from the POINT OF INTERSECTION of line  $r=2i-4j+2k + \lambda (3i+4j+2k)$  and plane r.(i-2j+k)=0.

### FORM- 5(A) EQUATION OF A LINE PERPENDICULAR TO TWO GIVEN LINES.

**Q.5** Find the equation of a LINE passes through (2,-1, 3) and PERPENDICULAR to the lines  $r = (i+j-k) = \lambda (2i-2j+k)$  and  $r = (2i-j-3k) + \mu (i+2j+2K)$ .

### FORM- 5(B) EQUATION OF A LINE PARALLEL TO TWO GIVEN PLANES.

**Q.6** Find the equation of a LINE passes through (1, 2, 3) and PARALLEL to the planes x-y+2z=5 and 3x+y+z=6.

### FORM-6(A) EQUATION OF A PLANE PERPENDICULAR TO TWO GIVEN PLANES.

**Q.7** Find the equation of a PLANE passes through (1,-1, 2) and is perpendicular to the planes 2x+3y-2z=5 and x+2y-3z=8.

# FORM-6(B) EQUATION OF A PLANE PARALLEL TO TWO GIVEN LINES.

**Q.8** Find the equation of a PLANE passes through (1, 2,-4) and parallel to the lines  $r=i+2j-4k+\lambda$  (2i+3j+6k) and  $r=i-3j+5k+\mu$  ( i+j-k).

# FORM-7 EQUATION OF A PLANE CONTAINING ONE OR TWO LINES.

**Q.9** Find the equation of a PLANE containing the lines  $r=2i+j-3k+\lambda$  (i+2j+5K) and  $r=3i+3j+2k+\mu$  (3i-2j+5k).

# FORM-8(A) DISTANCE OF A POINT FROM PLANE MEASURED PARALLEL TO A LINE.

**Q.10** Find the DISTANCE of the point (1,-2, 3) from the plane x- y+ z=5 measured parallel to the line  $r = i+3j-2k+\lambda$  (2i+3j - 6k).

# FORM- 8(B) DISTANCE OF A POINT FROM LINE MEASURED PARALLEL TO A PLANE.

**Q.11** Find the DISTANCE of the point (2, 3, 4) from the line  $r = -3i+2j+\lambda$  (3i+6j+2k) measured parallel to the plane 3x+2y+2z-5=0.

# FORM-9 IMAGE OF A LINE WITH RESPECT TO A PLANE.

**Q.12** Find the IMAGE of the line  $r=i+3j+4k+\lambda$  (3i+j-5k) in the plane 2x- y+z+3=0.

# FORM-10 FAMILY OF PLANES IN DIFFERENT CONDITIONS.

Q.13 Find the equation of a PLANE passing through the line of intersection of two planes and
A) a given passing point B)Perpendicular to a plane C) Parallel to a line or any axes. D) Relation between their intercepts. E) Perpendicular distance is given.

# !!..ANSWERS..!!

**Q.1** (-1,-6,-12) **Q.2** F(1,6,0) I(-3,8,-2) length= $2\sqrt{6}$  **Q.3** F(1,3,0) I(-1,4,-1) D= $\sqrt{6}$  **Q.4** 13 units **Q.5** r=2i-j+3k+ $\lambda$ (-6i-3j+6k) **Q.6** r= i+2j+3k + $\lambda$ (-3i+5j+4k) **Q.7** 5x-4y-z-7=0 **Q.8** 9x-8y+z+11=0 **Q.9** 10x+5y-4z=37 **Q.10** 1 unit **Q.11**)  $\sqrt{33}$  units **Q.12** r= -3i+5j+2k+ $\lambda$  (3i+j-5k).