

MATHEMATICS

Chapter 10: STRAIGHT LINES



STRAIGHT LINES



Some Important Results

- 1. The distance between two points A (x_1, y_1) and B (x_2, y_2) is given by $AB = \sqrt{(x_2 x_1)^2 + (y_2 y_1)^2}$
- **2.** The distance of a point P(x, y) from the origin is given by OP = $\sqrt{x^2, y^2}$.
- **3.** Let $A(x_1, y_1)$, $B(x_2, y_2)$ and $C(x_3, y_3)$ be the coordinates of the vertices of the triangle ABC. Then, the area of the triangle ABC is given by

Area =
$$\frac{1}{2} |x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)|$$

4. If the three points and, then $A(x_1,y_1)$, $B(x_2,y_2)$ and $C(x_3,y_3)$ are collinear, then

$$X_1(y_2 - y_3) + X_2(y_3 - y_1) + X_3(y_1 - y_2) = 0$$

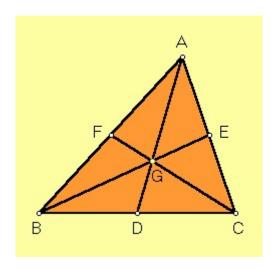
- **5.** Let A(x₁, y₁), and B(x₂, y₂) be two points. Then, the coordinates of the point P(x, y) which divides the line segment joining A and B internally in the ratio m:n are $\left(\frac{mx_2+nx_1}{m+n}, \frac{my_2+ny_1}{m n}\right)$.
- **6.** Let A(x₁, y₁), and B(x₂, y₂) be two points. Then the coordinates of the point P(x, y) that divides the line segment joining A and B externally in the ratio m:n are $\left(\frac{mx_2-nx_1}{m-n}, \frac{my_2-ny_1}{m n}\right)$.
- 7. Let A(x₁, y₁), and B(x₂, y₂) be two points. Then, the coordinates of the mid-point P(x, y) of the segment A and B are $\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$.
- **8.** line If the three points A(x₁, y₁), B(x₂,y₂) and C(x₃, y₃) are the vertices of the triangle ABC, then the coordinates of the centroid of the triangle are $\left(\frac{x_1+x_2+x_3}{3}, \frac{y_1+y_2+y_3}{3}\right)$.

Key concepts

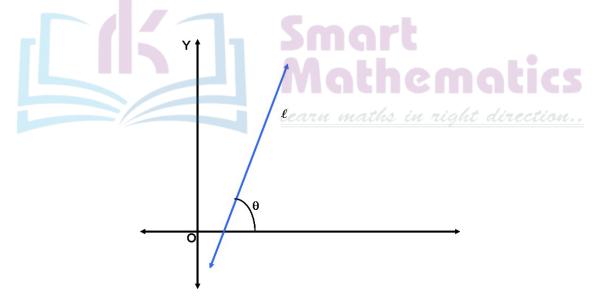
- **1.** For two points on a line parallel to X—axis, the distance between them is just the modulus of the difference between their x coordinates.
- **2.** For two points, on a line parallel to Y-axis the distance between them is just the modulus of the difference between their y coordinates.
- **3.** Three points are collinear, i.e., they lie on the same line if the triangle formed by them has zero area.

4. The centroid G divides the medians in the ratio 2:1. A triangle can be divided into 3 triangles of equalarea by its centroid Δ GAB, Δ GBC and Δ GAC are equal in area.





5. The angle (say) θ made by the line ℓ with positive direction of X-axis and measured anticlockwise is called the inclination of the line $0^{\circ} \le \theta \le 180^{\circ}$.



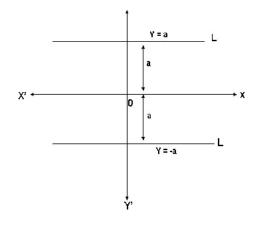
- 6. A line which is parallel to the X-axis or coinciding with the X-axis has inclination 0°.
- 7. A line that is parallel to the Y-axis or coinciding with the Y-axis has inclination 90°.
- 8. The slope of a straight line is a measure indicating its inclination with respect to the positive direction of the X-axis.
- 9. Consider a line not parallel to the Y-axis. If it makes an angle θ with the X-axis (measured in theanticlockwise direction), then m = tan θ is called the slope of the line.



- **10.** Slope of a line parallel to the Y-axis is not defined.
- **11.**Slope of a line parallel to the X-axis is zero.
- **12.**If the slope is positive, then the angle of inclination θ is an acute angle.
- **13.**If the slope is zero, then the line is X-axis or is parallel to X-axis.
- **14.**If the slope is negative, then the angle of inclination is an obtuse angle.
- **15.**Two lines are parallel, i.e., they never meet, if and only if one of the following conditions holds:
 - i. They are both vertical lines, i.e., they are parallel to the Y-axis.
 - ii. If their slopes are equal, i.e., $m_1 = m_2$.
- **16.**Two lines (not parallel to the Y-axis) are perpendicular if and only if their slopes m_1 and m_2 satisfies the condition that $m_1m_2 = -1$. If one of the lines is parallel to the Y-axis, i.e., a vertical line with its slope undefined, then any line parallel to the X-axis, i.e., a horizontal line with slope 0 is perpendicular to it.

Conversely, suppose a pair of lines, where one is horizontal and the other is vertical, then the given lines are perpendicular.

- **17.**If X, Y and Z are three points in the XY plane, then they are collinear if and only if slope of XY is the same as the slope of YZ.
- **18.**If θ is the inclination of a line L, then $\tan\theta$ is called the slope or gradient of the line L.
- **19.** If a horizontal line L is at a distance a units from the x-axis, then the ordinate of every point lying onthe line is a. Thus, the equation of such a line L is y = a where a is any real number.

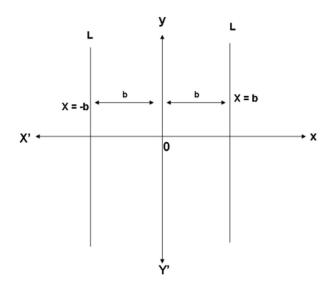


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20. Equation of a vertical line at a distance b from the Y-axis is x = b. Depending upon



whether the line is on the left or right of the Y-axis, the constant b is positive or negative.



- 21. Various forms of equation of the line
 - a. Slope intercept form
 - b. Point slope form
 - c. Two-point form
 - d. Intercept form
 - e. Normal form



22. The general equation of a straight line is Ax + By + C = 0, where A, B and C are constants and A and B are not zero simultaneously.

Case 1: $A \neq 0$, B = 0

In this case, the equation reduces to

$$Ax + C = 0 \text{ or } x = -\frac{C}{A}$$

which is a straight line parallel to the Y-axis.

Case 2: A = 0, $B \neq 0$ then as in case 1, the straight line is parallel to the X-axis.

$$By + C = 0$$

$$y = -\frac{C}{B}$$

Case 3: A \neq 0, B \neq 0

$$y = -\frac{A}{B} \times -\frac{C}{B}$$



which is the slope intercept form of a straight line with slope

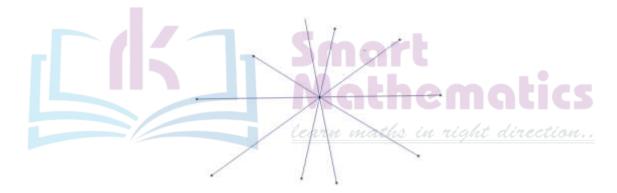
$$-\frac{A}{B}$$
 and $\,$ y- intercept $-\frac{C}{B}$

Case 4: If C = 0, then Ax + By + C = 0 becomes

$$Ax + By = 0.$$

This is a line passing through the origin and therefore line has zero intercepts on the axes.

- **23.** Equation of the line parallel to the line Ax + By + C = 0 is Ax + By + K = 0, where K is any arbitrary constant.
- **24.** Equation of line perpendicular to the line Ax + By + C = 0 is Bx Ay + K = 0.
- **25.**Two or more lines are concurrent if they meet at a single point.



- 26. General equation of line Ax + By + C=0 can be reduced to other forms of line as well
 - i. Slope intercept form:

If
$$B \neq 0$$
, then $Ax + By + C = 0$ can be written as

$$By = -Ax - C$$

$$\Rightarrow y = -\frac{A}{B} \times -\frac{C}{B}$$

ii. Intercept form: If $C \neq 0$, then Ax + By + C = 0

$$\Rightarrow$$
Ax + By = -C

$$\Rightarrow (\frac{A}{-C})x + (\frac{B}{-C})y = 1$$

$$\Rightarrow \frac{x}{\left(-\frac{C}{A}\right)} + \frac{y}{\left(-\frac{C}{B}\right)} = 1$$

$$\Rightarrow \frac{x}{a} + \frac{y}{b} = 1$$

iii. Normal form:

Ax + By + C = 0 or Ax + By = -C.

$$\Rightarrow \frac{A}{\cos \omega} = \frac{B}{\sin} = -\frac{C}{p}$$

$$\Rightarrow$$
 x cos ω + y sin ω = p

iv. Distance form:

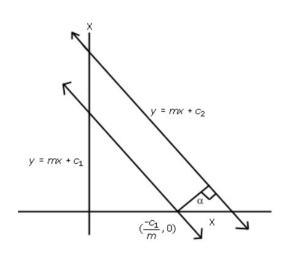
Let θ be the angle with the positive direction of X-axis is $\frac{x-x_1}{\cos\theta} = \frac{y-y_1}{\sin} = r, \text{ where } r \text{ is the distance of the point (x, y) on the line from the point (x₁, y).}$

27. The coordinates of any point on the line at a distance r from the point (x_1, y) are

$$(x_1 \pm r \cos \theta, y_1 \pm r \sin \theta)$$

- **28.** The slope of the line ax + by + c = 0 is $-\frac{a}{b} = -\frac{\text{coefficient of x}}{\text{coefficent of y}}$
- **29.**The distance of a point from a line is the length of perpendicular drawn from the point on the line.
 - **30.** Distance between two parallel lines is equal to the length of the perpendicular from a point to line (2). Therefore, the distance between parallel lines y = mx + c and y = mx + d is given by

Distance =
$$\frac{\left| (-m)(\frac{-c}{m}) + (-d) \right|}{\sqrt{1+m^2}} = \frac{|c-d|}{\sqrt{1+m^2}}$$



31. Let $L_1 = a_1x + b_1y + c_1 = 0$

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- $L_2 = a_2x + b_2y + c_2 = 0$ and
- $L_3 = a_3 x + b_3 y + c_3 = 0$ be three lines then they are concurrent if

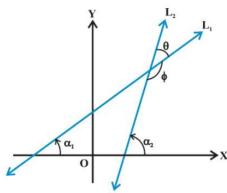
$$\begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix} = 0$$

- **32.**If two lines having the same slope pass through a common point, then the two lines will coincide.
- **33.**If θ is the inclination of a line ℓ , then tan θ is called the slope or gradient of the line ℓ .
- **34.**Two lines are parallel if and only if their slopes are equal.
- **35.**Two lines are perpendicular if and only if the product of their slopes is -1.
- **36.**The equation of the line having a normal distance from the origin p and angle between the normal and the positive X-axis ω is given by x cos ω + y sin ω = p.

Key formulae

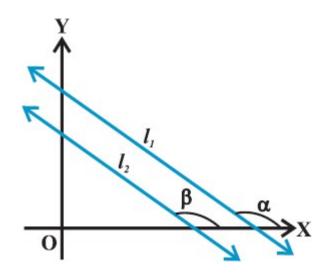
- 1. (a) If a line makes an angle á with the positive direction of X-axis, then the slope of the line is given by $\tan \theta \neq 90^{\circ}$.
 - (b) Slope or gradient of a line joining (x_1, y_1) , (x_2, y_2) is $m = \tan \theta = \frac{y_2 y_1}{x_2 x_1} = \frac{rise}{sun}$.
 - (c) Slope of the horizontal line is zero and slope of vertical line is undefined.
- **2.** Angle θ between two lines L_1 and L_2

$$\tan \theta = \left| \frac{m_2 - m_1}{1 + m_1 m} \right|, \text{ as } 1 + m_1 m_2 \neq 0$$



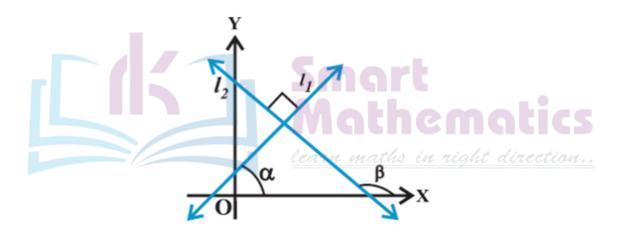
3. For parallel lines





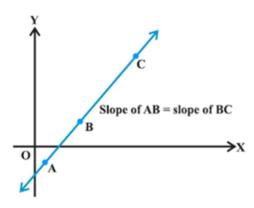
Slope of L_1 (m₁) = slope of L_2 (m₂) or tan α = tan β .

4. For perpendicular lines



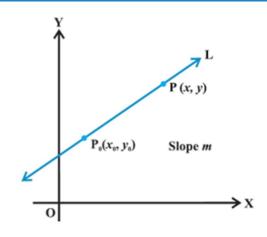
Slope of L_1 (m_1) × slope of L_2 (m_2) =-1, i.e., m_1m_2 = -1.

5. Three points are collinear if and only if the slope of AB = slope of BC.



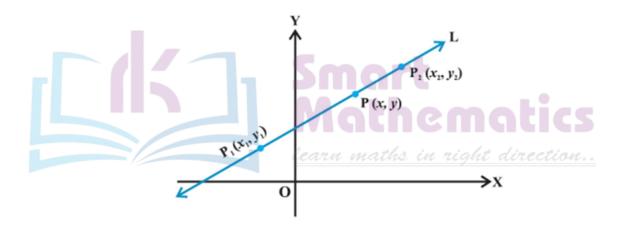
6. Point-slope form: $m = \frac{y-y_0}{x-x_0}$, i.e., y-y=m ($x-x_0$)



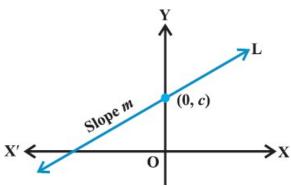


7. Two-point form: The equation of the line passing through the points (x_1, y_1) and (x_2, y_2) is given by

$$y - y_1 = \frac{y_2 - y_1}{x_2 - y_1} (x - x)$$



8. Slope-intercept form: Equation of line L with the point (x, y) and slope m and y-intercept c is y = mx + c.



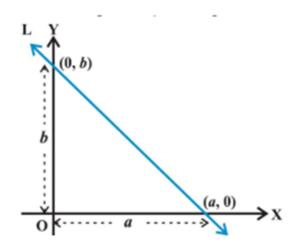
(b) Suppose line L with slope m makes x-intercept d. The equation of L is y = m(x - d).

9. Intercept form: Equation of the line making intercepts a and b on the X and Y-axis, respectively.





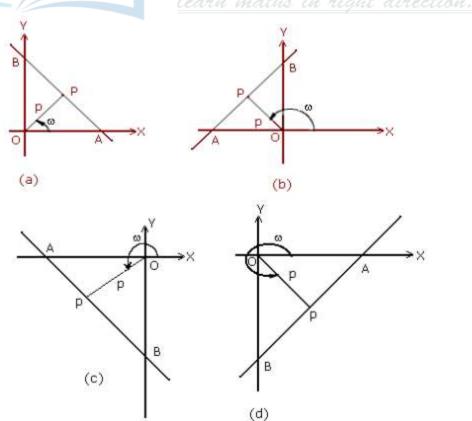
$$\frac{x}{a} + \frac{y}{b} = 1$$



10.Normal form: The equation of the line having normal distance p from the origin and angle to whichthe normal makes with the positive direction of x-axis is given by

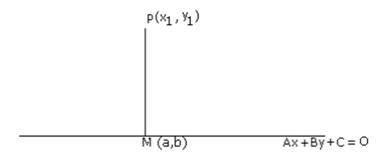
$$x \cos \omega + y \sin \omega = p$$





- 11. General orm of linear equation: Equation of the form Ax + By + C = 0, where A and B mothematics are not zerosimultaneously.
- **12.** The perpendicular distance (d) of a line Ax + By + C = 0 from a point $P(x_1, y_1)$ not on it is given by

$$d = \frac{\left|Ax_1 + By_1 + C\right|}{\sqrt{A^2 + C}}$$



13. Distance between two parallel lines $Ax + by + C_1 = 0$ and $Ax + By + C_2 = 0$ is given by

$$d = \frac{\left|C_1 - C_2\right|}{\sqrt{A^2 + C_2}}$$

- Mathematics

 learn maths in right direction...
- **14.** The equation of the lines passing through (x_1, y) and making an angle θ with the line y = mx + c by is given by

$$y - y_1 = \frac{m \pm tan\theta}{1 \mp mtan\theta} (x - x_1)$$

MIND MAP: LEARNING MADE SIMPLE CHAPTER - 10

lines $(m, m, \neq -1)$ and θ be the slopes of two intersecting If m, and m, are the Then two lines are parallel their slopes are equal. Thus, any line parallel to = mx + c is of the type y = mx + d, where d is any parameter

wo lines ax + by +c=0 and a'x + b'x + c' = 0 are parallel if $\frac{a}{a'} = \frac{b}{b'} \neq \frac{c}{c'}$

acute angle between them

 $= \frac{m_1 - m_2}{1 + m_1 m_2}$

then $\tan \theta =$

he distance between two parallel lines with equations $ax + by + c_1 = 0$

 $\frac{c_1 - c_2}{\sqrt{a^2 + b^2}}$ $ax + by + c_2 = 0$ is

=mx + c is of the form, $y = \frac{-1}{m}x + d$ where d is When two lines of the slope m, & m, are at right ngles, the Product of their slope is -1, i.e., $m_2 = -1$. Thus, any line perpendicular to ny parameter.

E TEMOTOPHO OF POPPER MANUSTRANS wo lines ax + by + c = 0 and a'x + b'y + c' = 0 are erpendicular to ax + by + c = 0 is of the form erpendicular if aa' + bb' = 0. Thus, any line x - ay + k = 0, where k is any parameter.

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səqols riəht do smrət ni sənil Angle between two straight

Distance Formula 2/8/16/11 30 ES/A

Fromma Gection

Straight Line

SLOPE INTERCEPT FORM: y = mx + c is the equation of a straight line whose slope is 'm' and Fquation of Equation of Straight Line in various forms tomorphistic or rest Still & HO THOOL MORE

perpendicular from ax + by + c = 0 is: The length of the imilarly, foot of perpendicular from a

 $ax_1 + by_1 + c$

 $y-y_1$

 $x-x_1$

 $\sqrt{a^2+b^2}$

he image of a point(x_1 , y_1) about a line

x + by + c = 0 is:

 $ax_1+by_+ c$ $\sqrt{a^2+b^2}$

 $-\left(ax_{1}+by_{1}+c\right)$

 $y-y_1$

 $x - x_1$

soint on the line is:

• If θ is the angle at which a straight line is inclined to be+ve of the line, denoted by m, is defined by $m = \tan \theta$. If θ is 90° , direction of x-axis and $0^{\circ} \le \theta < 180^{\circ}$, $\theta \ne 90^{\circ}$, then the slope *m* doesn't exist, but the line is parallel to *y*-axis. If $\theta = 0^{\circ}$, then m=0 and the line is parallel to x-axis.

then the slope *m* of the line is given by $m = (y_1 - y_2/x_1 - x_2)$ If $A(x_1, y_1)$ and $B(x_2, y_2)$, $x_1 \neq x_2$ are points on straight line,

Area of triangle whose vertices are (x_1, y_1) , (x_2, y_2) and (x_3, y_3) is $\frac{1}{2}(x_1(y_1 - y_2) + x_2(y_3 - y_1) + x_3(y_1 - y_2)$ The distance between the points $A(x_1, y_1)$ and $B(x_2, y_2)$ is $\sqrt{(x_1-x_2)^2+(y_1-y_2)^2}$

The P(x, y) divided the line joining A(x, y) and B(x, y) in the ratio $mx_2 + nx_1$. . . $my_2 + ny_1$ m:n, then $x = \frac{mx_2 + nx_1}{m + n}$, $y_1 = \frac{my_2 + nx_2}{m + n}$

Note: • If m/n is +ve, the division is internal, but if m/n is -ve, the division is external

• If m = n, then P is the mid-point of the line segment joining A & B. 1. **POINT-SLOPE FORM**: $y - y_1 = m(x - x_1)$ is the equation of a straight line whose slope is 'm' and passes through the point (x_1, y_1) .

3.TWO POINT FORM: $y - y_1 = \frac{y_2 - y_1}{x_2 - x_1}$ ($x - x_1$) is the equation of a straight line which passes makes an intercept c on the y-axis.

through $(x_1, y_1) & (x_2, y_2)$.

4. INTERCEPT FORM: $\frac{x}{a} + \frac{y}{b} = 1$ is the equation of a straight line which makes intercepts a & b on x and y axis respectively.

equation of a straight line where the length of the perpendicular from origin O on the line is p 5. **NORMAL** / **PERPENDICULAR FORM**: $x\cos\alpha + y\sin\alpha = p$ (where $p > 0, \le 0 \ \alpha < 2\pi$) is the and this perpendicular makes an angle α with +ve x-axis.

6. **GENERAL FORM**: ax + by + c = 0 is the equation of a straight line in general form. In this case, 2 2 = = - = of line



Important Questions



Multiple Choice questions-

Question 1. In a $\triangle ABC$, if A is the point (1, 2) and equations of the median through B and C are respectively x + y = 5 and x = 4, then B is

- (a) (1, 4)
- (b) (7, -2)
- (c) none of these
- (d) (4, 1)

Question 2. The equation of straight line passing through the point (1, 2) and perpendicular to the line x + y + 1 = 0

- (a) y x + 1 = 0
- (b) y x 1 = 0
- (c) y x + 2 = 0
- (d) y x 2 = 0

Question 3. The points (-a, -b), (0, 0), (a, b) and (a^2, ab) are

(a) vertices of a square

- (b) vertices of a parallelogram
- (c) collinear
- (d) vertices of a rectangle

Question 4. The equation of the line through the points (1, 5) and (2, 3) is

- (a) 2x y 7 = 0
- (b) 2x + y + 7 = 0
- (c) 2x + y 7 = 0
- (d) x + 2y 7 = 0

Question 5. The slope of a line which passes through points (3, 2) and (-1, 5) is

- (a) 3/4
- (b) -3/4
- (c) 4/3

Question 6. The ratio of the 7th to the $(n-1)^{th}$ mean between 1 and 31, when n arithmetic means are inserted between them, is 5:9. The value of n is

- (a) 15
- (b) 12
- (c) 13
- (d) 14

Question 7. The ortho centre of the triangle formed by lines xy = 0 and x + y = 1 is :

- (a) (0, 0)
- (b) none of these
- (c) (1/2, 1/2)
- (d) (1/3, 1/3)

Question 8. Two lines $a_1 x + b_1 y + c_1 = 0$ and $a_2 x + b_2 y + c_2 = 0$ are parallel if

- (a) $a_1/a_2 = b_1/b_2 \neq c_1/c_2$
- (b) $a_1/a_2 \neq b_1/b_2 = c_1/c_2$
- (c) $a_1/a_2 \neq b_1/b_2 \neq c_1/c_2$
- (d) $a_1/a_2 = b_1/b_2 = c_1/c_2$



Question 9. If the line x/a + y/b = 1 passes through the points (2, -3) and (4, -5), then (a, b) is

- (a) a = 1 and b = 1
- (b) a = 1 and b = -1
- (c) a = -1 and b = 1
- (d) a = -1 and b = -1

Question 10. The angle between the lines x - 2y = y and y - 2x = 5 is

- (a) tan⁻¹ (1/4)
- (b) $tan^{-1}(3/5)$
- (c) $tan^{-1} (5/4)$
- (d) $tan^{-1}(2/3)$

Very Short Questions:

- 1. Find the slope of the lines passing through the point (3,-2) and (-1,4)
- **2.** Three points P(h,k), $Q(x_1,y_1)$ and $R(x_2,y_2)$ lie on a line. Show that $(h-x_1)(y_2-y_1)=(k-y_1)(x_2-x_1)$

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3. Write the equation of the line through the points (1, -1) and (3, 5)



- **4.** Find the measure of the angle between the lines x + y + 7 = 0 and x y + 1 = 0.
- **5.** Find the equation of the line that has y-intercept 4 and is \perp to the line y = 3x 2.
- **6.** Find the equation of the line, which makes intercepts -3 and 2 on the x and y-axis respectively.
- 7. Equation of a line is 3x 4y + 10 = 0 find its slope.
- **8.** Find the distance between the parallel lines 3x 4y + 7 = 0 and 3x 4y + 5 = 0.
- 9. Find the equation of a straight line parallel to y-axis and passing through the point (4,-2)
- **10.** If 3x by + 2 = 0 and 9x + 3y + a = 0 represent the same straight line, find the values of a and b.

Short Questions:

1. If p is the length of the from the \perp origin on the line whose intercepts on the axes are a and b. show that

$$\frac{1}{p^2} = \frac{1}{a^2} + \frac{1}{b^2}$$

- 2. Find the value of p so that the three lines 3x + y 2 = 0, px + 2y 3 = 0 and may intersect at one point.
- **3.** Find the equation to the straight line which passes through the point (3,4) and has intercept on the axes equal in magnitude but opposite in sign.
- **4.** By using area of Δ . Show that the points (a, b + c), and (c, a + b) are collinear.
- **5.** Find the slope of a line, which passes through the origin, and the midpoint of the line segment joining the point p(0, 4) and Q(8, 0)

Long Questions:

- 1. Find the values of for the line $(k-3)x (4 k^2)y + k^2 7k + 6 = 0$
 - (a). Parallel to the x-axis
 - (b). Parallel to y-axis
 - (c). Passing through the origin.
- **2.** If p and q are the lengths of \perp from the origin to the lines.

$$x\cos\theta - y\sin\theta = k\cos 2\theta$$
, and $x\sec\theta + y\cos ec\theta = k$ respectively, prove that $p^2 + 4q^2 = k^2$

- **3.** Prove that the product of the \perp drawn from the points $(\sqrt{a^2 b^2}, 0)$ and $(-\sqrt{a^2 b^2}, 0)$ to the line.
- **4.** Find equation of the line mid way between the parallel lines 9x + 6y 7 = 0 and 3x + 2y + 6 = 0.

5. Assuming that straight lines work as the plane mirror for a point, find the image of the point (1,2) in the line x - 3y + 4 = 0.

Assertion Reason Questions:

- 1. In each of the following questions, a statement of Assertion is given followed by a corresponding statement of Reason just below it. Of the statements, mark the correct answer as.
 - **Assertion (A):** The point (3, 0) is at 3 units distance from the Y -axis measured along the positive X -axis and has zero distance from the X -axis.
 - **Reason (R):** The point (3, 0) is at 3 units distance from the X -axis measured along the positive Y -axis and has zero distance from the Y -axis.
 - (i) Both assertion and reason are true and reason is the correct explanation of assertion.
 - (ii) Both assertion and reason are true but reason is not the correct explanation of assertion.
 - (iii) Assertion is true but reason is false.
 - (iv) Assertion is false but reason is true.
- 2. In each of the following questions, a statement of Assertion is given followed by a corresponding statement of Reason just below it. Of the statements, mark the correct answer as.
 - Assertion (A): Slope of X -axis is zero and slope of Y -axis is not defined.
 - **Reason (R):** Slope of X -axis is not defined and slope of Y -axis is zero.
 - (i) Both assertion and reason are true and reason is the correct explanation of assertion.
 - (ii) Both assertion and reason are true but reason is not the correct explanation of assertion.
 - (iii) Assertion is true but reason is false.
 - (iv) Assertion is false but reason is true.

Answer Key:

MCQ

- **1.** (b) (7, -2)
- **2.** (b) y x 1 = 0
- 3. (c) collinear
- **4.** (c) 2x + y 7 = 0
- **5.** (b) -3/4



- **6.** (d) 14
- **7.** (a) (0, 0)
- **8.** (a) $a_1/a_2 = b_1/b_2 \neq c_1/c_2$
- **9.** (d) a = -1 and b = -1
- **10.**(c) tan⁻¹ (5/4)

Very Short Answer:

1. Slope of line through (3,-2) and (-1, 4)

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$=\frac{4-(-2)}{-1-3}$$

$$=\frac{6}{-4}=\frac{-3}{2}$$

2. Since P, Q, R are collinear

Slope of PQ = slope of QR

$$\frac{y_1 - k}{x_1 - h} = \frac{y_2 - y_1}{x_2 - x_1}$$

$$\frac{\sum (k - y_1)}{\sum (h - x_1)} = \frac{y_2 - y_1}{x_2 - x_1}$$

$$(h-x_1)(y_2-y_1)=(k-y_1)(x_2-x_1)$$

3.

$$y-y_1 = \frac{y_2-y_1}{x_2-x_1} \left(x-x_1 \right)$$
 Req. eq.

$$y+1=\frac{5+1}{2}(x-1)$$

$$-3x+y+4=0$$

4.

$$x + y + 7 = 0$$

$$m_1 = \frac{-1}{1}$$

$$x - y + 1 = 0$$

$$m_2 = \frac{-1}{-1} = 1$$

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Slopes of the two lines are 1 and -1 as product of these two slopes is -1, the lines are at right angles.

5.

$$y=3x-2$$

Slope
$$(m) = \frac{-3}{-1} = 3$$
, slope of any line \perp it is $-\frac{1}{3}$

$$C = 4$$

Req. eq. is
$$y = mx + c$$

$$y = \frac{-1}{3}x + 4$$

6.

$$\operatorname{Req. eq.} \frac{x}{a} + \frac{y}{b} = 1$$

$$a = -3, b = 2$$

$$\therefore \frac{x}{-3} + \frac{y}{2} = 1$$

$$2x - 3y + 6 = 0$$

7.

$$m = \frac{-\text{coff. of } x}{\text{coff. of } y}$$

$$=\frac{-3}{-4}=\frac{3}{4}$$

8.

$$A = 3, B = -4, C_1 = 7$$
 and $C_2 = 5$

$$d = \frac{|C_1 - C_2|}{\sqrt{a^2 + b^2}}$$

$$=\frac{|7-5|}{\sqrt{(3)^2+(-4)^2}}$$

$$=\frac{2}{5}$$

9.

Equation of line parallel to y-axis is x = a....(i)

Smart Mathematics



$$a = -4$$

So
$$x = -4$$

$$x + 4 = 0$$

10.

ATQ

$$\frac{3}{9} = \frac{-b}{3} = \frac{2}{a}$$

$$b = -1$$

$$\Rightarrow a = 6$$

Short Answer:

1. Equation of the line is $\frac{x}{a} + \frac{y}{b} = 1$

$$\Rightarrow \frac{x}{a} + \frac{y}{b} - 1 = 0$$

The distance of this line from the origin is P

$$\therefore P = \frac{\left| \frac{0}{a} + \frac{0}{b} - 1 \right|}{\sqrt{\left(\frac{1}{a}\right)^2 + \left(\frac{1}{b}\right)^2}}$$

$$\frac{P}{1} = \frac{1}{\sqrt{\frac{1}{a^2} + \frac{1}{b^2}}}$$

$$\frac{1}{P} = \sqrt{\frac{1}{a^2} + \frac{1}{b^2}}$$

Sq. both side

$$\frac{1}{P^2} = \frac{1}{a^2} + \frac{1}{b^2}$$

2.

$$3x + y - 2 = 0....(i)$$

$$px + 2y - 3 = 0....(ii)$$

$$2x - y + 3 = 0$$
.....(iii)

On solving eq. (i) and (iii)

$$x = 1$$
, And $y = -1$



Put
$$x, y$$
 in eq. (ii)

$$P(1) + 2(-1) - 3 = 0$$

$$p-2-3=0$$

$$p = 5$$

3.

Let intercept be a and -a the equation of the line is

$$\frac{x}{a} + \frac{y}{-a} = 1$$

$$\Rightarrow x - y = a....(i)$$

Since it passes through the point (3, 4)

$$3 - 4 = a$$

$$a = -1$$

Put the value of a in eq. (i)

$$x-y=-1$$

$$x - y + 1 = 0$$

4.

arn maths in right direction..

$$= \frac{1}{2} |a(c+a)-b(b+c)+b(a+b)-c(c+a)+c(b+c)-a(a+b)|$$

$$=\frac{1}{2}.0=0$$

5.

 $M = \left(\frac{0+8}{2}, \frac{-4+0}{2}\right)$ Let m be the midpoint of segment PQ then

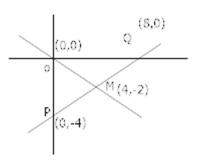
$$=(4,-2)$$

$$OM = \frac{y_2 - y_1}{x_2 - x_1}$$

Slope of

$$=\frac{-2-0}{4-0}=\frac{-1}{2}$$





Long Answer:

1. (a) The line parallel to x-axis if coeff. Of x = 0

$$k - 3 = 0$$

$$k = 3$$

(b) The line parallel to y-axis if coeff. Of y=0

$$4 - k^2 = 0$$

$$k = \pm 2$$

(c) Given line passes through the origin if (0, 0) lies on given eq.

$$(k-3) \cdot (0) - (4-k^2)(0) + k^2 - 7k + 6 = 0$$

$$(k-6)(k-1)=0$$

$$k = 6.1$$

2.

$$P = \frac{|0.\cos\theta - 0\sin\theta - k\cos 2\theta|}{\sqrt{(\cos\theta)^2 + (-\sin\theta)^2}} \begin{bmatrix} \bot \text{ from origin} \\ \because (0,0) \end{bmatrix}$$

$$P = K \cos 2\theta(i)$$

$$q = \frac{|0.\sec\theta + 0\cos ec\theta - k|}{\sqrt{\sec^2\theta + \cos ec^2\theta}}$$

$$= \frac{K}{\sqrt{\frac{1}{\cos^2 \theta} + \frac{1}{\sin^2 \theta}}}$$

$$= \frac{k \cos \theta \cdot \sin \theta}{\sqrt{\sin^2 \theta + \cos^2 \theta}} = \frac{1}{2} k \cdot \sin \theta \cdot \cos \theta$$

$$2q = k \cdot \sin 2\theta \cdot \dots \cdot (ii)$$

Squaring (i) and (ii) and adding

$$P^2 + (2q)^2 = K^2 \cos^2 2\theta + K^2 \sin^2 2\theta$$



$$P^{2} + 4q^{2} = K^{2} (\cos^{2} 2\theta + \sin^{2} 2\theta)$$

 $p^{2} + 4q^{2} = k^{2}$

3. Let

$$p_1 = \frac{\left| \frac{\sqrt{a^2 - b^2}}{a} \cdot \cos \theta - 1 \right|}{\sqrt{\left(\frac{\cos \theta}{a}\right)^2 + \left(\frac{\sin \theta}{b}\right)^2}} \left[\because \bot \text{ from the points } \sqrt{a^2 - b^2}, 0 \right]$$

Similarly p_2 be the distance $\left(-\sqrt{a^2-b^2},0\right)$ from to given line

$$p_2 = \frac{\left| -\frac{\sqrt{a^2 - b^2}}{a} \cos \theta - 1 \right|}{\sqrt{\left(\frac{\cos \theta}{a}\right)^2 + \left(\frac{\sin \theta}{b}\right)^2}}$$

$$p_{1}p_{2} = \frac{\left|\frac{\sqrt{a^{2}-b^{2}}}{a}\cos\theta - 1\right| \left(-\frac{\sqrt{a^{2}-b^{2}}}{a}\cos\theta - 1\right)}{\frac{\cos^{2}\theta}{a^{2}} + \frac{\sin^{2}\theta}{b^{2}}}$$

$$= \frac{\left|\frac{a^{2}-b^{2}}{a^{2}}\right| \cdot \cos^{2}\theta - 1}{\frac{b^{2}\cos^{2}\theta + a^{2}\sin^{2}\theta}{a^{2}b^{2}}}$$
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$$= \frac{\left| a^{2} \cos^{2} \theta - b^{2} \cos^{2} \theta - a^{2} \right| a^{2} b^{2}}{a^{2} (a^{2} \sin^{2} \theta + b^{2} \cos^{2} \theta)}$$

$$= \frac{\left|-(a^2 \sin^2 \theta + b^2 \cos^2 \theta)\right| b^2}{a^2 \sin^2 \theta + b^2 \cos^2 \theta} \qquad \left[\because a^2 \cos^2 \theta - a^2 = a^2 (\cos^2 \theta - 1)\right]$$

$$=\frac{(a^2\sin^2\theta+b^2\cos^2\theta)\ b^2}{a^2\sin^2\theta+b^2\cos^2\theta}$$

$$= b^2$$

4.

The equations are

$$9x + 6y - 7 = 0$$

$$3\left(3x+2y-\frac{7}{3}\right)=0$$



$$3x + 2y - \frac{7}{3} = 0.....(i)$$

$$3x + 2y + 6 = 0....(ii)$$

Let the eq. of the line mid way between the parallel lines (i) and (ii) be

$$3x + 2y + k = 0....(iii)$$

ATQ

Distance between (i) and (iii) = distance between (ii) and (iii)

$$\left| \frac{K + \frac{7}{3}}{\sqrt{9+4}} \right| = \left| \frac{K-6}{\sqrt{9+4}} \right| \quad \left[\because d = \frac{|c_1 - c_2|}{\sqrt{a^2 + b^2}} \right]$$

$$K + \frac{7}{3} = K - 6$$

$$K = \frac{11}{6}$$

Req. eq. is

$$3x + 2y + \frac{11}{6} = 0$$

Mathematics

5.

Let Q(h, k) is the image of the point p(1, 2) in the line.

$$x-3y+4=0.....(i)$$

 $PQ = \left(\frac{h+1}{2}, \frac{k+2}{2}\right)$ Coordinate of midpoint of

This point will satisfy the eq.(i)

$$\left(\frac{h+1}{2}\right) - 3\left(\frac{k+2}{2}\right) + 4 = 0$$

$$h-3k = -3.....(i)$$

(Slope of line PQ) × (slope of line x - 3y + 4 = 0) = -1

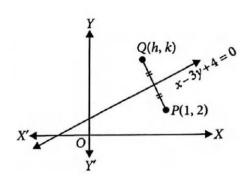
$$\left(\frac{k-2}{h-1}\right)\left(\frac{-1}{-3}\right) = -1$$

$$3h + k = 5.....(ii)$$

On solving (i) and (ii)

$$h = \frac{6}{5} \quad \text{and} \quad k = \frac{7}{5}$$





Assertion Reason Answer:

- 1. (iii) Assertion is true but reason is false.
- 2. (iii) Assertion is true but reason is false.

